

# DOING THINGS WITH DERIVATIVES

Math 130 - Essentials of Calculus

8 October 2019

## COMPUTING SECOND DERIVATIVES

## EXAMPLE

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②  $f(x) = x^3 - 4x + 6$

③  $g(t) = (t - 2)(2t + 3)$

## BASIC PHYSICS

If  $s(t)$  is a position function, then the velocity is given by  $v(t) = s'(t)$  and acceleration is given by  $a(t) = v'(t) = s''(t)$ .

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- 3 At what times does the object change direction?

# TANGENT LINES

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Find the tangent line to the given function at the given point.

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❷  $f(x) = x + \sqrt{x}$  at  $(4, 6)$

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- 2  $\sqrt[3]{26}$

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*If  $C(v)$  is the cost, in dollars, of purifying  $v$  gallons of drinking water, and  $C'(200000) = 0.26$ , estimate the cost of purifying an additional 3000 gallons of water once 200,000 gallons have been processed.*